

Name : First name:

Ain M'Lila 14/01/2026

Metrology 2 quality 1 exam

Choose the correct answer: (29 pts)

<p>1. In physics, making a measurement means:</p> <p>A. Finding the exact value of a physical quantity</p> <p>B. Estimating a quantity without instruments</p> <p>(1,5 pt) <input checked="" type="radio"/> C. Determining the numerical value of a physical quantity</p> <p>D. Eliminating all measurement errors</p>	<p>2. Why is it impossible to know the exact (true) value of a quantity?</p> <p>A. Because instruments do not exist</p> <p>(1,5 pt) <input checked="" type="radio"/> B. Because measurement errors are unavoidable</p> <p>C. Because calculations are incorrect</p> <p>D. Because scientists do not agree</p>
<p>3. Measurement error is defined as:</p> <p>A. The uncertainty of the instrument</p> <p>(1,5 pt) <input checked="" type="radio"/> B. The difference between the measured value and the true value</p> <p>C. The variation of repeated measurements</p> <p>D. The precision of the instrument</p>	<p>4. Why is the measurement error itself unknown?</p> <p>A. Because the measured value is incorrect</p> <p>B. Because the instrument is poorly calibrated</p> <p>(1,5 pt) <input checked="" type="radio"/> C. Because the true value is unknown</p> <p>D. Because measurements are not repeated</p>
<p>5. What is used to judge the precision of a measurement?</p> <p>A. The true value</p> <p>B. The measurement error</p> <p>(1,5 pt) <input checked="" type="radio"/> C. The unit of measurement</p> <p>(1,5 pt) <input checked="" type="radio"/> D. The measurement uncertainty</p>	<p>6. Measurement uncertainty represents:</p> <p>A. The exact value of the quantity</p> <p>(1,5 pt) <input checked="" type="radio"/> B. An interval where the true value is likely to be found</p> <p>C. A mistake made during measurement</p> <p>D. The instrument resolution only</p>

Problem

Let consider the following equations:

$$f(x, y, z) = x\sqrt{z - y}$$

$$g(x, y, z) = x^3 + \sqrt{y} - \sqrt{z}$$

Data:

With: $x = 5.08 \pm 0.17$; $y = 12.6 \pm 0.2$; $z = 19.31 \pm 0.06$

- Give the value of $f(x, y, z)$ and its uncertainty (using the GUM method)
- Give the value of $g(x, y, z)$ and its uncertainty (using the GUM method)
- Which error is dominating in $g(x, y, z)$ function?

Pr K Bouche

Problem (Corrected) 41 pt

✓ $f(x, y, z) = x\sqrt{z-y}$ calculation of f : $f = 13,16$ 0,5 pt

$\frac{\partial f}{\partial x} = \sqrt{z-y}$ 0,5 pt; $\frac{\partial f}{\partial y} = -\frac{x}{2\sqrt{z-y}}$ 0,5 pt

$\frac{\partial f}{\partial z} = \frac{x}{2\sqrt{z-y}}$ 0,5 pt

$\begin{cases} \frac{\partial f}{\partial x} \approx 2,59 & \text{0,5 pt} \\ \frac{\partial f}{\partial y} \approx -0,98 & \text{0,5 pt} \\ \frac{\partial f}{\partial z} \approx 0,98 & \text{0,5 pt} \end{cases}$

0,5 pt $\Delta f = \sqrt{\left(\frac{\partial f}{\partial x} \Delta x\right)^2 + \left(\frac{\partial f}{\partial y} \Delta y\right)^2 + \left(\frac{\partial f}{\partial z} \Delta z\right)^2} = \sqrt{(2,59 \times 0,17)^2 + (-0,98 \times 0,2)^2 + (0,98 \times 0,26)^2}$

$\Rightarrow \Delta f = 0,49$ 0,5 pt so, $f = 13,16 \pm 0,49$ 0,5 pt

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✓ $g(x, y, z) = x^3 + \sqrt{y} - \sqrt{z}$ calculating g : $g = 130,16$ 0,5 pt

$\frac{\partial g}{\partial x} = 3x^2 \approx 77,4$ 0,5 pt

$\frac{\partial g}{\partial y} = \frac{1}{2\sqrt{y}} \approx 0,141$ 0,5 pt

$\frac{\partial g}{\partial z} = -\frac{1}{2\sqrt{z}} \approx -0,141$ 0,5 pt

0,5 pt $\Delta g = \sqrt{\left(\frac{\partial g}{\partial x} \Delta x\right)^2 + \left(\frac{\partial g}{\partial y} \Delta y\right)^2 + \left(\frac{\partial g}{\partial z} \Delta z\right)^2} = \sqrt{(77,4 \times 0,17)^2 + (0,141 \times 0,2)^2 + (-0,141 \times 0,26)^2}$

0,5 pt $\Delta g = 13,16$ so $g = 130,16 \pm 13,16$ 0,5 pt

✓ the dominating error in g function is $\left[\frac{\partial g}{\partial x} \Delta x\right]$ 0,5 pt
equal to $77,4 \times 0,17 = 13,158 \approx 13,16$ 0,5 pt