

Module: Antennas and radiation

FINAL EXAM

G:.....

surname&first name:.....

course questions: (08 pts)

- give the expression for the radiation intensity U and that for the radiation density P_{ray}

$$U(\theta, \phi) = \frac{P_{\text{ray}}}{4\pi} (\text{W/Sr})$$

- what is the difference between gain and directivity

$$G = D / \pi$$

- Mention the three radiation zones and their limits.

1/ Rayleigh zone $R < 0.62 \sqrt{D/\lambda}$

2/ near Field zone $0.62 \sqrt{D/\lambda} < R < 2D/\lambda$ (Fresnel)

3/ Far Field zone $R > 2D/\lambda$ (Fraunhofer)

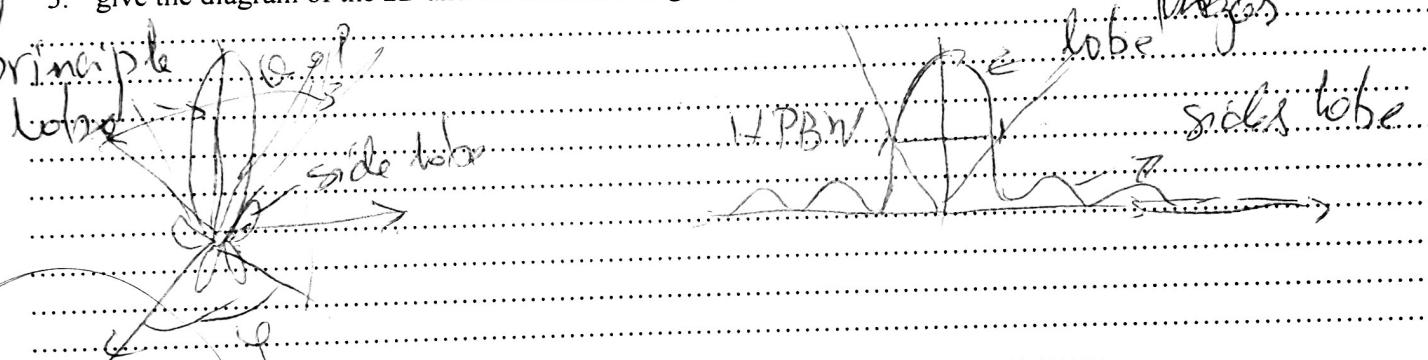
- Name the three modes of polarization of an electromagnetic wave.

..> linear

..> circular

..> elliptical

- give the diagram of the 2D and 3D radiation diagram, citing the different parts

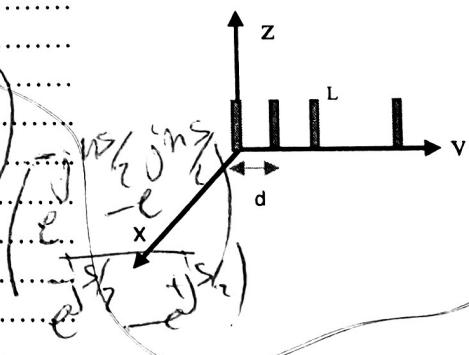


- We consider N vertical antennas, spaced d apart and powered by currents of the same amplitude and the same phase

- Give the expression for the modulus of the E field radiated by this grouping

$$\begin{aligned} E_{\text{tot}} &= E_1 + E_2 + E_3 + \dots + E_N \\ &= E_1 (1 + e^{j\phi_2} + e^{j\phi_3} + \dots + e^{j\phi_N}) \\ &= E_1 (1 - e^{-j\pi}) + e^{j\phi_2} + e^{j\phi_3} + \dots + e^{j\phi_N} \\ &= E_1 e^{j\phi_1} \left(\frac{e^{-j\pi}}{1 - e^{-j\pi}} + 1 + e^{j\phi_2} + e^{j\phi_3} + \dots + e^{j\phi_N} \right) \\ &= E_1 e^{j\phi_1} \frac{\sin(N\pi/2)}{\sin(\pi/2)} \end{aligned}$$

$$S = \beta d \sin \phi \sin \phi$$



- Define total characteristic function (radiation)

$$F(\theta, \varphi) = F_r(\theta) \cdot C(\theta, \varphi) / C(\theta, \varphi) = \frac{\sin \frac{n\pi}{2}}{\sin \frac{n\pi}{2}}$$

Exercise 01

An antenna emits a signal with a total power of 10 watts. We measure a radiation intensity which follows the following expression:

$$U(\theta, \varphi) = \begin{cases} B \cdot \cos^2(\theta) [\text{W/sr}] & \text{pour } 0 \leq \theta \leq \frac{\pi}{2}; \text{ et } -\pi \leq \varphi \leq +\pi \\ 0 & \text{ailleurs} \end{cases}$$

- Find the correct value of B
- Determine the surface power density at a distance of 1000m
- Find the maximum directivity in value and dB

Exercise 02

An isotropic antenna radiates a power of 20W at 5cm wavelength. Determine :

- antenna gain
- The transmission frequency.
- The radiated power density at 100 km.
- Radiation intensity

Exercise 03:

We consider a uniform network of 2 identical Hertz doublets of length $2L$ (same amplitude of the supply current), regularly spaced by a distance d . Knowing that these doublets are parallel and are contained in the same yoz plane, the current

$$I(z) = I_M e^{j\omega z}$$

- Give the expression for the field of antenna 2?
- Give the expression for the total field?
- Deduce the characteristic radiation function of the group? knowing

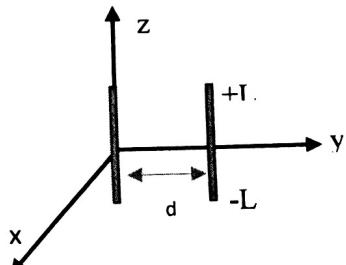
$$\text{that } F_i(\theta) = \frac{\cos(\frac{\pi}{2} \cos \theta)}{\sin \theta}$$

$$E_2 = E_1 e^{j\omega z} \quad / s = \beta d \sin \theta \sin \varphi$$

$$E_{\text{tot}} = E_1 + E_2 = E_1 + E_1 e^{j\omega z}$$

$$= E_1 e^{j\omega z} \left(1 + e^{j\omega z} \right)$$

$$F(\theta, \varphi) = F_r(\theta) \cdot C(\theta, \varphi) = \frac{100 \left(\frac{1}{2} \sin \theta \right)}{\sin \theta} \cdot \cos \left(\frac{\theta}{2} \right) \cdot \cos \left(\frac{\varphi}{2} \right)$$



$$U(\theta, \varphi) = \begin{cases} B \cdot \cos^2(\theta) [w/sr] & \text{pour } 0 \leq \theta \leq \frac{\pi}{2}; \text{ et } -\pi \leq \varphi \leq +\pi \\ 0 & \text{ailleurs} \end{cases}$$

1. Trouver la valeur de B qui convient
2. Déterminer la densité surfacique de puissance à une distance de 1000m
3. Trouver la directivité maximale en valeur et en dB

$$\begin{aligned} P_{rad} &= \iint_{\Omega} U(\theta, \varphi) d\Omega = \iint B \cos^2 \theta \sin \varphi d\theta d\varphi \quad / \quad (\cos^2 \theta)' = -2 \cos \theta \sin \theta \\ &= B \int_{-\pi}^{\pi} d\varphi \int_0^{\pi} 3 B \cos^2 \theta \sin \theta d\theta = -B (2\pi) \left[\frac{\cos^3 \theta}{3} \right]_0^{\pi} = B \frac{2\pi}{3} = \end{aligned}$$

$$\Rightarrow B = \frac{15}{\pi} \quad (un)$$

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M1 S2

Module : Antennes et rayonnements

$$2/ P = \frac{U(\theta, \phi)}{R^2} = \frac{15}{\pi/10} \cos \theta \cdot \cos \phi \text{; } R = 10 \text{ m}$$

..... allors

$$3/ P_{max} = 4\pi \cdot U_{max} = 4\pi \cdot 15 = 60; P_{max \text{ dB}} = 7,78 \text{ dB}$$

Exercice 02

Une antenne isotrope rayonne une puissance de 20W à 5cm de longueur d'onde. Déterminer :

- Le gain de cette antenne.
- La fréquence d'émission.
- L'intensité de rayonnement
- La densité de puissance rayonnée à 100 Km.

$$a) G = 1; \lambda = 0,05 \text{ m}$$

$$b) f = \frac{c}{\lambda} = \frac{3 \cdot 10^8}{0,05} = 6 \cdot 10^9 \text{ Hz}$$

$$G = \frac{P(\theta, \phi)}{P_{max}} = 1 \Rightarrow U(\theta, \phi) = P_{max} = 1,5 \text{ W/m}^2$$

$$d) P_{ray} = \frac{U}{R^2} = \frac{P_{max} G e}{4\pi d^2} = \frac{20}{4\pi (10^5)^2} = 1,5 \cdot 10^{-10} \text{ (W/m}^2)$$

Exercice 03:

..... les suivants :