

## QCM (8 pts)

1. Which field is least likely to use decision support? B)
2. What is a model? B)
3. What does a zero-sum game imply? B)
4. What does Alpha–Beta pruning do? B)
5. When does decision-making under uncertainty occur? B)
6. What defines a decision problem under uncertainty? B)
7. What does the Minimax Regret criterion aim to do? B)
8. If  $\alpha = 0$  in the Hurwicz criterion, it becomes which method? B)
9. Which criterion is considered balanced and realistic? C)
10. What is an expert system? B)
11. What is a key feature of expert systems? A)
12. Which inference method starts from known facts? A)
13. What is a disadvantage of forward chaining? A)
14. What is an advantage of expert systems? A)
15. Which is an example of a benefit criterion in MCDM? A)
16. What does a heuristic evaluation function do? A)

### Exercise 01 (4pts) – Decision under Uncertainty

#### Payoff Matrix (k\$)

Action	s <sub>1</sub>	s <sub>2</sub>	s <sub>3</sub>
a <sub>1</sub>	120	60	20
a <sub>2</sub>	90	70	30
a <sub>3</sub>	50	40	10

#### 1. Maximin Criterion (1pts)

Minimum payoff for each action:

- a<sub>1</sub> → min = **20**
- a<sub>2</sub> → min = **30**
- a<sub>3</sub> → min = **10**

**Optimal decision:** a<sub>2</sub> (maximum of minima = 30)

#### 2. Minimax Regret (Savage) (1.5)

Best payoff per state:

- s<sub>1</sub> → 120
- s<sub>2</sub> → 70
- s<sub>3</sub> → 30

#### Regret Matrix

Action	s <sub>1</sub>	s <sub>2</sub>	s <sub>3</sub>	Max Regret
a <sub>1</sub>	0	10	10	<b>10</b>
a <sub>2</sub>	30	0	0	30
a <sub>3</sub>	70	30	20	70

**Optimal decision:** a<sub>1</sub> (minimum regret = 10)

#### 3. Hurwicz Criterion ( $\alpha = 0.6$ )(1.5)

Hurwicz =  $\alpha \times \text{Max} + (1 - \alpha) \times \text{Min}$

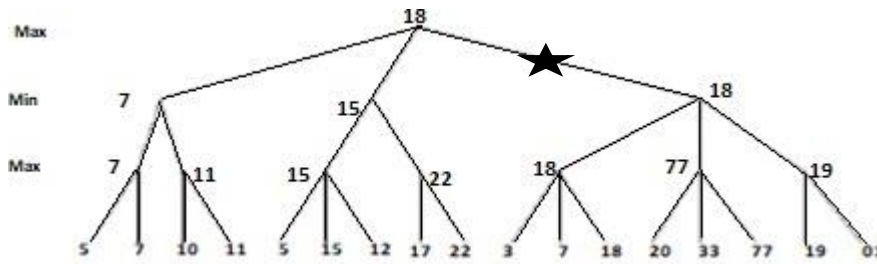
- a<sub>1</sub> =  $0.6 \times 120 + 0.4 \times 20 = \mathbf{80}$
- a<sub>2</sub> =  $0.6 \times 90 + 0.4 \times 30 = \mathbf{66}$
- a<sub>3</sub> =  $0.6 \times 50 + 0.4 \times 10 = \mathbf{34}$

**Optimal decision:** a<sub>1</sub>

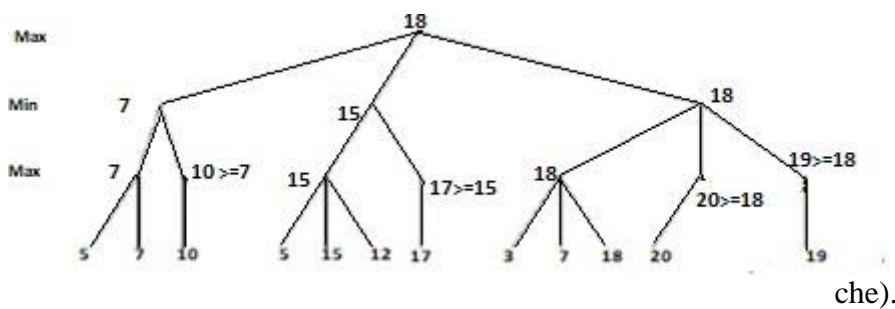
**Exercise 02 (4.5pts)– Minimax & Alpha-Beta**

*It is necessary to mention the value of alpha and beta at each node.*

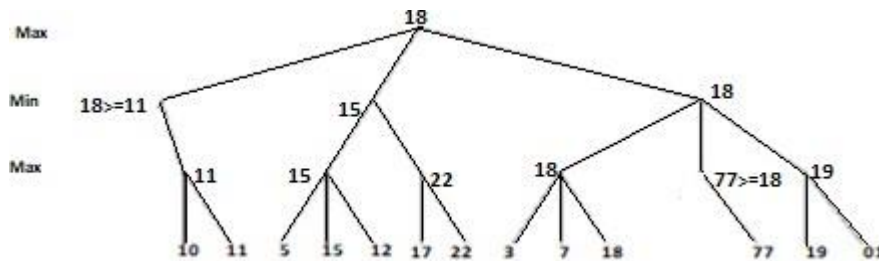
1. Appliquez l’algorithme minimax à l’arbre précédent (0.5).



2. Appliquez l’algorithme  $\alpha$ - $\beta$  sur l’arbre de décision (exploration à gauche).(1.5)



3. Appliquez l’algorithme  $\alpha$ - $\beta$  sur l’arbre de décision (exploration à droite).(1.5)



4. Explain the results obtained. What do you conclude? (1)

We observe that the two exploration orders do not yield the same results (in terms of subtree pruning). More generally, the order in which nodes are evaluated influences the performance of the alpha-beta algorithm (this opens the way to possible optimizations, particularly in the sorting of nodes during the construction of the game tree).

**Exercise 03 (3.5pts)– MCDM (Weighted Sum Method)**

**Problem Context**

You must choose the best car among **A, B, and C** based on **four criteria** with given weights.

**Criteria and Weights**

Criterion	Type	Weight
Price (kDA)	Cost	0.35
Fuel Consumption (L/100 km)	Cost	0.25
Comfort (/10)	Benefit	0.25
Safety (/10)	Benefit	0.15

**Step 1: Initial Decision Matrix**

Car	Price	Consumption	Comfort	Safety
A	250	5.5	8	9
B	300	4.8	9	8

C	220	6.0	7	7
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### Min and Max Values

Criterion	Min	Max
Price	220	300
Consumption	4.8	6.0
Comfort	7	9
Safety	7	9

### Normalized Decision Matrix (on 10) (1.5pts)

Use formula:

For a Cost criterion:

$$\text{Normalized Score} = \frac{\text{Max value} - \text{Value}}{\text{Max value} - \text{Min value}} \times 10$$

For a Benefit criterion :

$$\text{Normalized Score} = \frac{\text{Value} - \text{Min value}}{\text{Max value} - \text{Min value}} \times 10$$

Car	Price (Cost)	Consumption (Cost)	Comfort (Benefit)	Safety (Benefit)
A	6.25	4.17	5.00	10.00
B	0.00	10.00	10.00	5.00
C	10.00	0.00	0.00	0.00

### Step 5: Weighted Sum Method (WSM)(1.5pt)

WSM =  $\Sigma(\text{weight} \times \text{normalized score})$

#### Calculations

- Car A  $(6.25 \times 0.35) + (4.17 \times 0.25) + (5 \times 0.25) + (10 \times 0.15) = 5.98$
- Car B  $(0 \times 0.35) + (10 \times 0.25) + (10 \times 0.25) + (5 \times 0.15) = 5.75$
- Car C  $(10 \times 0.35) + (0) + (0) + (0) = 3.50$

### Final Ranking (0.5)

1. 1st: A, 2nd: B, 3rd: C