

Typical answer key for the STM1 S1 2023/2024 Exam

Level: 1st Year LMD C.S

Matter: STM1

Date : Jan 15, 2024

Exercise 1: (4 pts)

1. The choice of an answer:

$(10100111,1011)_2 =$ a) $(B7,B)_{16}$ b) $(167,6875)_{10}$ c) $(257,55)_8$ **(0.5 pt)**

$(737,61)_8 =$ a) $(1DF,C4)_{16}$ b) $(480,765)_{10}$ c) $(11111110,110001)_2$ **(0.5 pt)**

$(AD5,D8)_{16} =$ a) $(101011100101,11011)_2$ b) $(2774,85)_{10}$ c) $(5325,66)_8$ **(0.5 pt)**

$(167,6875)_{10} =$ a) $(A7,B)_{16}$ b) $(267,55)_8$ c) $(10110111,1011)_2$ **(0.5 pt)**

2. The answer with ‘Yes’ or ‘No’

| | |
|------------|-----------------|
| Yes | (0.5 pt) |
| No | (0.5 pt) |
| Yes | (0.5 pt) |
| Yes | (0.5 pt) |

Exercise 2: (4 pts)

1. A) $(64)_{10} = (01000000)_2$ **(0.25)**, $(128)_{10} = (10000000)_2$ **(0.25)**

B) **Sign and Absolute Value:** $[-(2^{n-1} - 1), +(2^{n-1} - 1)] \Leftrightarrow [-127, +127]$ **(0.25)**

$-64 \in [-127, +127] \Rightarrow -64 \equiv 11000000$ (S.V.A) **(0.25)**

$-128 \in [-127, +127] \Rightarrow$ we cannot represent it in S.A.V. **(0.25)**

C) **1's Complement:** $[-(2^{n-1} - 1), +(2^{n-1} - 1)] \Leftrightarrow [-127, +127]$ **(0.25)**

$-64 \in [-127, +127] \Rightarrow -64 \equiv 10111111$ (C.à.1) **(0.25)**

$-128 \in [-127, +127] \Rightarrow$ we cannot represent it in 1's Complement. **(0.25)**

D) **2's Complement:** $[-2^{n-1}, +(2^{n-1} - 1)] \Leftrightarrow [-128, +127]$ **(0.25)**

$-64 \in [-128, +127] \Rightarrow -64 \equiv 10111111 + 1 = 11000000$ (C.à.2) **(0.25)**

$-128 \in [-128, +127] \Rightarrow -128 \equiv 01111111 + 1 = 10000000$ (C.à.2) **(0.25)**

2. $(C5)_{16} = (?)_{10}$

$$\begin{array}{cc} & (C5)_{16} \\ \swarrow & \searrow \\ 1100 & 0101 \end{array} \quad (0.25)$$

$\Rightarrow (C5)_{16} = (11000101)_{c.à.2}$

$(11000101)_{c.à.2}$ is negative \Rightarrow we will find the positive value.

$$\begin{array}{r}
 11000101 \\
 - \quad \quad \quad 1 \\
 \hline
 11000100 \\
 \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \\
 00111011 \text{ (positif) } \mathbf{(0.25)}
 \end{array}$$

$(00111011)_{c.a.2} = (00111011)_2$
 $(00111011)_2 = 0 \times 2^7 + 0 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$
 $= 0 + 0 + 32 + 16 + 8 + 0 + 2 + 1$
 $= (59)_{10}$
 $\Rightarrow (00111011)_{c.a.2} = (+59)_{10} \quad \mathbf{(0.25)}$
 $\Rightarrow (C5)_{16} = (11000101)_{c.a.2}$
 $= (-59)_{10} \quad \mathbf{(0.25)}$

3. $1101001 - 1010111 = \mathbf{0010010} \quad \mathbf{(0.25 \text{ pt})}, \quad 10011101 \div 111 = \mathbf{10110.01101} \quad \mathbf{(0.25 \text{ pt})}$

Exercice 3 : (6 pts)

1. ASCII code

a) The values in base 10 corresponding to the binary numbers:

- A: $01000001 = 65 \quad \mathbf{(0.5 \text{ pt})}$; B: $01000010 = 66 \quad \mathbf{(0.5 \text{ pt})}$; C: $01000011 = 67 \quad \mathbf{(0.5 \text{ pt})}$
- a: $01100001 = 97 \quad \mathbf{(0.5 \text{ pt})}$; b: $01100010 = 98 \quad \mathbf{(0.5 \text{ pt})}$; c: $01100011 = 99 \quad \mathbf{(0.5 \text{ pt})}$

b) The ASCII codes of 'D' and 'd':

$$D: 01000100 = (68)_{10} \quad \mathbf{(0.5 \text{ pt})}; \quad d: 01100100 = (100)_{10} \quad \mathbf{(0.5 \text{ pt})}$$

2. $(642)_{10} = (0110 0100 0010)_{BCD} \quad \mathbf{(0.5 \text{ pt})}, \quad (3514)_{10} = (0011 0101 0001 0100)_{BCD} \quad \mathbf{(0.5 \text{ pt})}$

3. $(0110)_2 = (0101)_{GRAY} \quad \mathbf{(0.5 \text{ pt})}, \quad (1101)_2 = (1011)_{GRAY} \quad \mathbf{(0.5 \text{ pt})}$

Exercice 4:

1. The function $f(x, y, z)$

a) Canonical sum of minterms form:

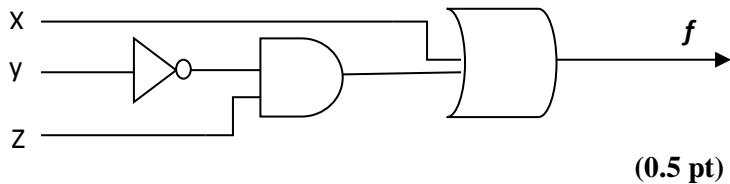
$$\begin{aligned}
 f(x, y, z) &= x + \bar{y}z \oplus \\
 &= x(y + \bar{y})(z + \bar{z}) + (x + \bar{x})\bar{y}z \\
 &= xyz + xy\bar{z} + x\bar{y}z + x\bar{y}\bar{z} + \bar{x}\bar{y}z \quad \mathbf{(1.25 \text{ pt})}
 \end{aligned}$$

b) Truth table: $\quad \mathbf{(1.25 \text{ pt})}$

| x | y | z | $f(x, y, z)$ |
|---|---|---|--------------|
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 |
| 0 | 1 | 0 | 0 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 |

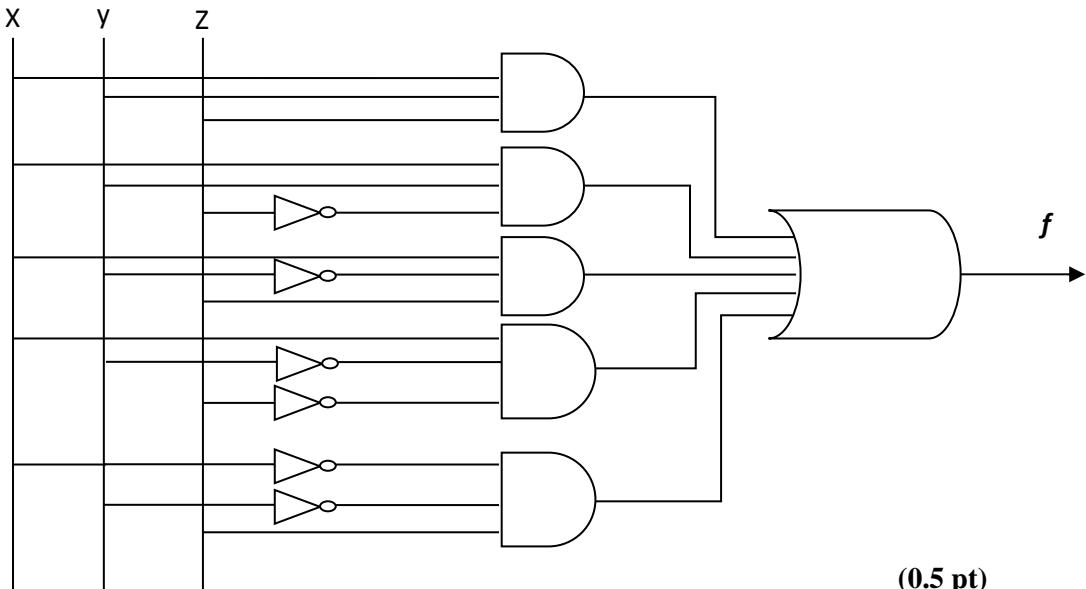
c) Logical diagram

1st expression



(0.5 pt)

2nd expression



(0.5 pt)

2. Answering course questions

- a) The goals of simplifying logic functions are:
 - Minimize the cost (0.5 pt)
 - Accelerate treatment (0.5 pt)
- b) The simplification methods are:
 - The algebraic method (0.5 pt)
 - The Karnaugh table method (0.5 pt)
 - The Quine/McCluskey method (0.5 pt)