



$$\begin{array}{r}
 11000101 \\
 - \quad \quad \quad 1 \\
 \hline
 11000100 \\
 \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \\
 \end{array}$$

00111011 (positif) (0.25)

$$(00111011)_{c.a.2} = (00111011)_2$$

$$\begin{aligned}
 (00111011)_2 &= 0 \times 2^7 + 0 \times 2^6 + 1 \times 2^5 + 1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 \\
 &= 0 + 0 + 32 + 16 + 8 + 0 + 2 + 1 \\
 &= (59)_{10}
 \end{aligned}$$

$$\Rightarrow (00111011)_{c.a.2} = (+59)_{10} \quad (0.25)$$

$$\begin{aligned}
 \Rightarrow (C5)_{16} &= (11000101)_{c.a.2} \\
 &= (-59)_{10} \quad (0.25)
 \end{aligned}$$

3.  $1101001 - 1010111 = \mathbf{0010010}$  (0.25 pt),  $10011101 \div 111 = \mathbf{10110.01101}$  (0.25 pt)

### Exercise 3 : (6 pts)

1. ASCII code

a) The values in base 10 corresponding to the binary numbers:

- A: 01000001 = 65 (0.5 pt); B: 01000010 = 66 (0.5 pt); C: 01000011 = 67 (0.5 pt)
- a: 01100001 = 97 (0.5 pt); b: 01100010 = 98 (0.5 pt); c: 01100011 = 99 (0.5 pt)

b) The ASCII codes of 'D' and 'd':

$$D: 01000100 = (68)_{10} \quad (0.5 \text{ pt}); \quad d: 01100100 = (100)_{10} \quad (0.5 \text{ pt})$$

2.  $(642)_{10} = (0110 \ 0100 \ 0010)_{BCD}$  (0.5 pt),  $(3514)_{10} = (0011 \ 0101 \ 0001 \ 0100)_{BCD}$  (0.5 pt)

3.  $(0110)_2 = (0101)_{GRAY}$  (0.5 pt),  $(1101)_2 = (1011)_{GRAY}$  (0.5 pt)

### Exercise 4:

1. The function  $f(x, y, z)$

a) Canonical sum of minterms form:

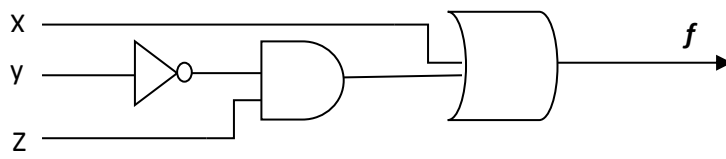
$$\begin{aligned}
 f(x, y, z) &= x + \bar{y} \cdot z \\
 &= x(y + \bar{y})(z + \bar{z}) + (x + \bar{x})\bar{y}z \\
 &= xyz + xy\bar{z} + x\bar{y}z + x\bar{y}\bar{z} + \bar{x}\bar{y}z \quad (1.25 \text{ pt})
 \end{aligned}$$

b) Truth table: (1.25 pt)

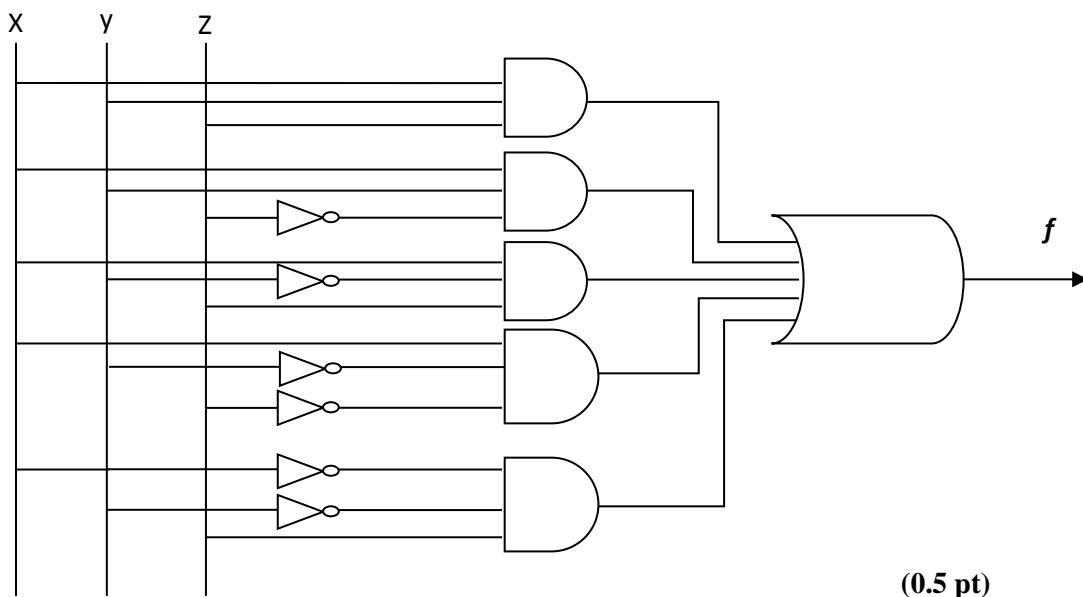
x	y	z	$f(x, y, z)$
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1

c) Logical diagram

1<sup>st</sup> expression



2<sup>nd</sup> expression



## 2. Answering course questions

a) The goals of simplifying logic functions are:

- Minimize the cost (0.5 pt)
- Accelerate treatment (0.5 pt)

b) The simplification methods are:

- The algebraic method (0.5 pt)
- The Karnaugh table method (0.5 pt)
- The Quine/McCluskey method (0.5 pt)