

Pts	الجواب (من مطبوعة الدروس و حلول التمارين)	N°
1	<p>مبدأ استبعاد باولي</p> $\Psi(\dots, x_i, \dots, x_j, \dots) = \theta \Psi(\dots, x_j, \dots, x_i, \dots) : \theta = \pm 1$ $\theta^2 = 1 \Rightarrow \Psi(\dots, x_i, \dots, x_j, \dots) ^2 = \Psi(\dots, x_j, \dots, x_i, \dots) ^2$ <p>لا تتغير كثافة احتمال وجود النظام عندما تتبادل الجسيمات ، لا يمكن تمييز الجسيمات المتطابقة.</p>	a
1	$\Psi(\dots, m_i, \dots, m_i, \dots) = -\Psi(\dots, m_i, \dots, m_i, \dots) = 0 : \theta = -1$	b
1	$W_{MB} \{ n_m \} = N! \prod_{m=1}^{\infty} \frac{g_m^{n_m}}{n_m!} , \text{ avec } \sum_{m=1}^{\infty} n_m = N$	c1
1	$W_{BE} \{ n_m \} = \prod_{m=1}^{\infty} \frac{(n_m + g_m - 1)!}{n_m! (g_m - 1)!} , \text{ avec } \sum_{m=1}^{\infty} n_m = N$	c2
1	$W_{FD} \{ n_m \} = \prod_{m=1}^{\infty} \frac{g_m!}{n_m! (g_m - n_m)!} , \text{ avec } \sum_{m=1}^{\infty} n_m = N$	c3
1	$P_m = \begin{cases} \frac{1}{\Omega} & \text{si } E \leq E_m \leq E + \Delta E \\ 0 & \text{ailleurs} \end{cases}$	d1
1	$\Omega(N, V, E; \Delta E) = \sum_{\text{Etats tq } 0 \leq E_m \leq E} 1 = \frac{1}{N! h^{sN}} \int_{EP \text{ tq } 0 \leq H(q,p) \leq E} d^{sN} q d^{sN} p$	d2
1	$P_m = \frac{g_m e^{-\beta E_m}}{Z}$	e1
1	$Z(N, V, \beta) = \sum_m e^{-\beta E_m} \rightarrow \frac{1}{N! h^{sN}} \int_{EP} d^{sN} q d^{sN} p e^{-\beta H(q, p)}$	e2
1	$P_{mN} = \frac{g_m e^{-\beta E_m N + \beta \mu N}}{\mathcal{E}}$	f1
2	$\mathcal{E} = \sum_{N=0}^{\infty} \sum_m e^{-\beta E_m N + \beta \mu N} = \sum_{N=0}^{\infty} \frac{e^{\beta \mu N}}{N! h^{sN}} \int_{EP} d^{sN} q d^{sN} p e^{-\beta H_N(q, p)}$	f2
1	$E = ME = M\epsilon_0 = (N_+ N_-) \epsilon_0 \text{ avec } N = N_+ + N_-$ $W(E) \equiv W_M = \frac{N!}{N_+! N_-!} = \frac{N!}{\left[\frac{1}{2}(N - M) \right]! \left[\frac{1}{2}(N + M) \right]!}$	1.
2	$S = k_B \log[W_M]$ $= k_B \left\{ N \log N - \left[\frac{1}{2}(N - M) \right] \log \left[\frac{1}{2}(N - M) \right] - \left[\frac{1}{2}(N + M) \right] \log \left[\frac{1}{2}(N + M) \right] \right\}$	
2	$\frac{1}{T} = \frac{\partial S}{\partial E} = \frac{\partial S}{\partial M} \frac{\partial M}{\partial E} = \frac{1}{\epsilon_0} \frac{\partial S}{\partial M} = \frac{1}{2} \frac{k_B}{\epsilon_0} \log \frac{(N - M)}{(N + M)}$ $E = M\epsilon_0 = (N_+ - N_-) \epsilon_0 = -N \tanh \left(\frac{\epsilon_0}{k_B T} \right)$	2.
2	$Z_1 = e^{\beta \epsilon_0} + e^{-\beta \epsilon_0} \quad \text{et} \quad Z_N = \left[2 \cosh \left(\frac{\epsilon_0}{k_B T} \right) \right]^N$	3.
1	$F = -k_B T \log(Z_N) = -N k_B T \log \left\{ 2 \cosh \left(\frac{\epsilon_0}{k_B T} \right) \right\}$	